

CHAPTER

7

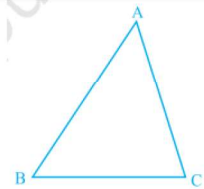
IX-MATHEMATICS-NCERT-2024-25

7. TRIANGLES (notes)

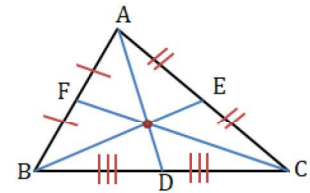
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<https://sureshmathsmaterial.com>

1. A closed figure formed by three intersecting lines is called a triangle.
2. A triangle has three sides, three angles and three vertices.
3. AB, BC, CA are the three sides, $\angle A$, $\angle B$, $\angle C$ are the three angles and A, B, C are three vertices
4. Triangle ABC, denoted as ΔABC



5. **Median:** A median connects a vertex of a triangle to the mid-point of the opposite side.
6. **congruent figures:** The figures that have the same shape and size are called congruent figures



Ex: (i) Two circles of the same radii are congruent

(ii) Two squares of the same sides are congruent.

7. The two triangles are congruent If the sides and angles of one triangle are equal to the corresponding sides and angles of the other triangle.
8. If ΔPQR is congruent to ΔABC , we write $\Delta PQR \cong \Delta ABC$.
9. $FD \leftrightarrow AB$, $DE \leftrightarrow BC$ and $EF \leftrightarrow CA$ and $F \leftrightarrow A$, $D \leftrightarrow B$ and $E \leftrightarrow C$. So, $\Delta FDE \cong \Delta ABC$.
10. Congruent triangles corresponding parts are equal and we write in short 'CPCT' for corresponding parts of congruent triangles.

Criteria for Congruence of Triangles

SAS congruence rule : Two triangles are congruent if two sides and the included angle of one triangle are equal to the two sides and the included angle of the other triangle

SAS congruence rule holds but not ASS or SSA rule.

Example 1 : In Fig. 7.8, $OA = OB$ and $OD = OC$. Show that (i) $\Delta AOD \cong \Delta BOC$ and (ii) $AD \parallel BC$

Sol: (i) In ΔAOD and ΔBOC

$$OA = OB \text{ (Given)}$$

$$OD = OC \text{ (Given)}$$

$$\angle AOD = \angle BOC \text{ (Vertically opposite angles)}$$

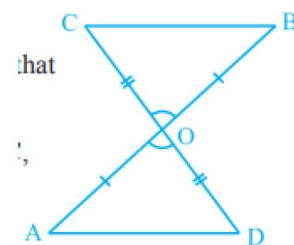
$$\Delta AOD \cong \Delta BOC \text{ (by the SAS congruence rule)}$$

(ii) Since $\Delta AOD \cong \Delta BOC$

$$\angle OAD = \angle OBC \text{ (CPCT)}$$

Alternate interior angles are equal

$$\therefore AD \parallel BC$$



Example 2 : AB is a line segment and line l is its perpendicular bisector. If a point P lies on l , show that P is equidistant from A and B .

Sol: l is perpendicular bisector of AB

ΔPCA and ΔPCB .

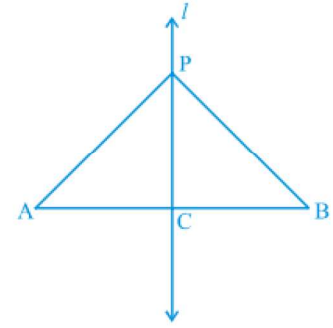
$AC = BC$ (C is midpoint of AB)

$\angle PCA = \angle PCB = 90^\circ$ ($l \perp AB$)

$PC = PC$ (Common)

So, $\Delta PCA \cong \Delta PCB$ (SAS congruence rule)

$PA = PB$ (CPCT)



ASA congruence rule : Two triangles are congruent if two angles and the included side of one triangle are equal to two angles and the included side of other triangle.

AAS and SAA are same as ASA congruence rule.

Example 3 : Line-segment AB is parallel to another line-segment CD . O is the mid-point of AD (see Fig. 7.15). Show that (i) $\Delta AOB \cong \Delta DOC$ (ii) O is also the mid-point of BC .

Sol: In ΔAOB and ΔDOC .

$\angle ABO = \angle DCO$ (Alternate interior angles)

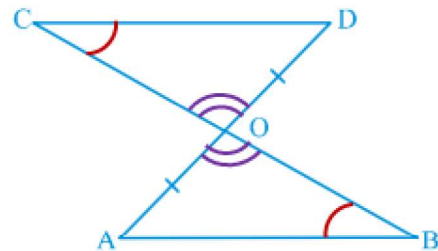
$OA = OD$ (Given)

$\angle AOB = \angle DOC$ (Vertically opposite angles)

$\therefore \Delta AOB \cong \Delta DOC$ (AAS rule)

$OB = OC$ (CPCT)

So, O is the mid-point of BC .



EXERCISE 7.1

1. In quadrilateral $ACBD$, $AC = AD$ and AB bisects $\angle A$ (see Fig. 7.16). Show that $\Delta ABC \cong \Delta ABD$.
What can you say about BC and BD ?

Sol: In ΔABC and ΔABD

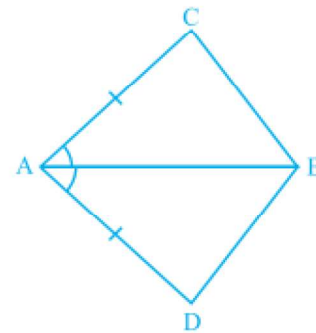
$AC = AD$ (Given)

$\angle BAC = \angle BAD$ (AB bisects $\angle A$)

$AB = AB$ (Common)

$\Delta ABC \cong \Delta ABD$ (SAS congruency rule)

$BC = BD$ (CPCT)



2. $ABCD$ is a quadrilateral in which $AD = BC$ and $\angle DAB = \angle CBA$ (see Fig. 7.17). Prove that
(i) $\Delta ABD \cong \Delta BAC$ (ii) $BD = AC$ (iii) $\angle ABD = \angle BAC$.

Sol: (i) In ΔABD and ΔBAC

$AD = BC$ (Given)

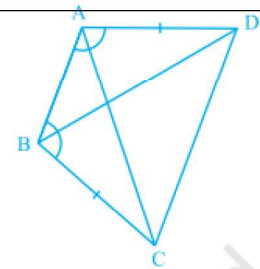
$\angle DAB = \angle CBA$ (Given)

$$AB=AB \text{ (Common)}$$

$$\Delta ABD \cong \Delta BAC \text{ (SAS congruence rule)}$$

$$(ii) \Delta ABD \cong \Delta BAC \Rightarrow BD = AC \text{ (CPCT)}$$

$$(iii) \Delta ABD \cong \Delta BAC \Rightarrow \angle ABD = \angle BAC \text{ (CPCT)}$$



3. **AD and BC are equal perpendiculars to a line segment AB (see Fig. 7.18). Show that CD bisects AB.**

Sol: In ΔOAD and ΔOBC

$$\angle OAD = \angle OBC = 90^\circ \text{ (Given)}$$

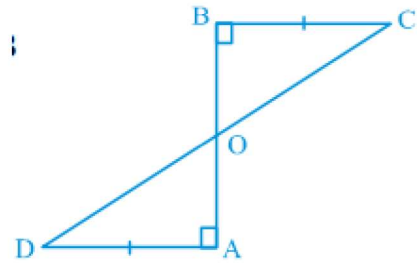
$$\angle AOD = \angle BOC \text{ (Vertically opposite angles)}$$

$$AD=BC \text{ (Given)}$$

$$\Delta OAD \cong \Delta OBC \text{ (AAS congruence rule)}$$

$$OA=OB$$

\therefore CD bisects AB.



4. **l and m are two parallel lines intersected by another pair of parallel lines p and q (see Fig. 7.19). Show that $\Delta ABC \cong \Delta CDA$.**

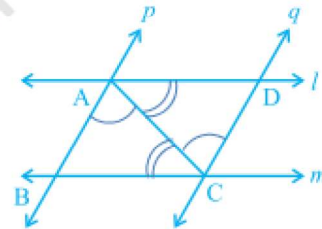
Sol: In ΔABC and ΔCDA

$$\angle BAC = \angle DCA \text{ (} p \parallel q, \text{ Alternate interior angles)}$$

$$AC=AC \text{ (Common)}$$

$$\angle BCA = \angle DAC \text{ (} l \parallel m, \text{ Alternate interior angles)}$$

$$\Delta ABC \cong \Delta CDA \text{ (By ASA congruence rule)}$$



5. **Line l is the bisector of an angle $\angle A$ and B is any point on l. BP and BQ are perpendiculars from B to the arms of $\angle A$ (see Fig. 7.20). Show that: (i) $\Delta APB \cong \Delta AQB$ (ii) $BP = BQ$ or B is equidistant from the arms of $\angle A$.**

Sol: (i) In ΔAPB and ΔAQB

$$\angle BAP = \angle BAQ \text{ (} l \text{ is the angle bisector of } \angle A \text{)}$$

$$AB=AB \text{ (Common)}$$

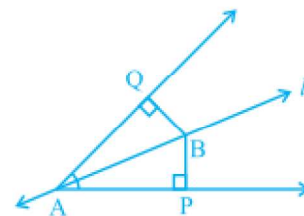
$$\angle APB = \angle AQB = 90^\circ$$

$$\Delta APB \cong \Delta AQB \text{ (By ASA congruence rule)}$$

$$(ii) \Delta APB \cong \Delta AQB$$

$$BP=BQ \text{ (By CPCT)}$$

B is equidistant from the arms of $\angle A$

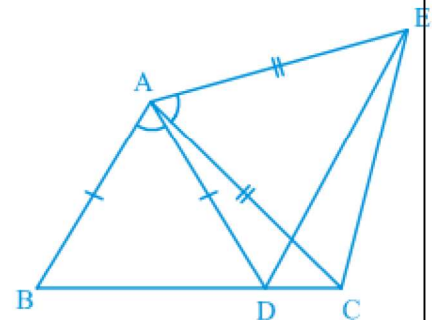


6. **In Fig. 7.21, $AC = AE$, $AB = AD$ and $\angle BAD = \angle EAC$. Show that $BC = DE$.**

Sol: $\angle BAD = \angle EAC$ (Given)

$$\angle BAD + \angle DAC = \angle EAC + \angle DAC$$

$$\angle BAC = \angle DAE \rightarrow (1)$$



In $\triangle BAC$ and $\triangle DAE$

$AB = AD$ (Given)

$\angle BAC = \angle DAE$ (From (1))

$AC = AE$ (Given)

$\triangle BAC \cong \triangle DAE$ (By SAS congruence rule)

$\therefore BC = DE$ (By CPCT)

7. **AB is a line segment and P is its mid-point. D and E are points on the same side of AB such that $\angle BAD = \angle ABE$ and $\angle EPA = \angle DPB$ (see Fig. 7.22). Show that (i) $\triangle DAP \cong \triangle EBP$ (ii) $AD = BE$**

Sol: $\angle EPA = \angle DPB$ (given)

$\angle EPA + \angle DPE = \angle DPB + \angle DPE$

$\therefore \angle APD = \angle BPE \rightarrow (1)$

In $\triangle APD$ and $\triangle BPE$

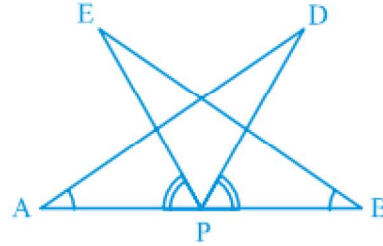
$\angle BAD = \angle ABE$ (Given)

$AP = BP$ (P is midpoint of AB)

$\angle APD = \angle BPE$ (From (1))

$\triangle APD \cong \triangle BPE$ (By ASA congruence rule)

$\therefore AD = BE$ (By CPCT)



8. **In right triangle ABC, right angled at C, M is the mid-point of hypotenuse AB. C is joined to M and produced to a point D such that $DM = CM$. Point D is joined to point B (see Fig. 7.23). Show that: (i) $\triangle AMC \cong \triangle BMD$ (ii) $\angle DBC$ is a right angle. (iii) $\triangle DBC \cong \triangle ACB$ (iv) $CM = \frac{1}{2}AB$**

Sol: (i) In $\triangle AMC$ and $\triangle BMD$

$AM = BM$ (M is midpoint of AB)

$\angle AMC = \angle BMD$ (Vertically opposite angles)

$DM = CM$ (Given)

$\therefore \triangle AMC \cong \triangle BMD$ (By SAS congruence rule)

(ii) $\triangle AMC \cong \triangle BMD$

$\angle ACM = \angle BDM$ (By CPCT)

Alternate interior angles are equal

$\therefore DB \parallel AC$

$\angle DBC + \angle ACB = 180^\circ$ (co-interior angles are supplementary)

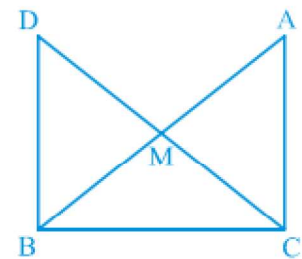
$\angle DBC + 90^\circ = 180^\circ$ (Given $\angle ACB = 90^\circ$)

$\therefore \angle DBC = 90^\circ$

(iii) In $\triangle DBC$ and $\triangle ACB$

$DB = AC$ ($\triangle AMC \cong \triangle BMD$)

$\angle DBC = \angle ACB = 90^\circ$



$$BC=CB \text{ (common)}$$

$$\Delta DBC \cong \Delta ACB \text{ (By SAS congruence rule)}$$

$$\text{(iv) } \Delta DBC \cong \Delta ACB$$

$$AB=DC \text{ (by CPCT)}$$

$$AB=2 \text{ CM (CM=DM)}$$

$$CM = \frac{1}{2}AB$$

Some Properties of a Triangle

Theorem 7.2 : Angles opposite to equal sides of an isosceles triangle are equal.

Sol: ΔABC is an isosceles triangle in which $AB=AC$

Draw AD is angle bisector of $\angle A$

In ΔBAD and ΔCAD

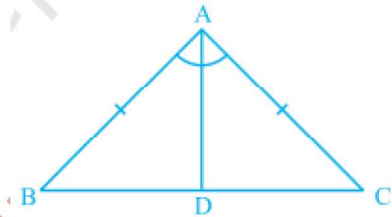
$$AB = AC \quad \text{(Given)}$$

$$\angle BAD = \angle CAD \text{ (By construction)}$$

$$AD = AD \quad \text{(Common)}$$

So, $\Delta BAD \cong \Delta CAD$ (By SAS rule)

$$\angle B = \angle C \text{ (CPCT)}$$



Theorem 7.3 : The sides opposite to equal angles of a triangle are equal.

Proof: In ΔABC , $\angle B = \angle C$

Draw AD is angle bisector of $\angle A$

In ΔBAD and ΔCAD

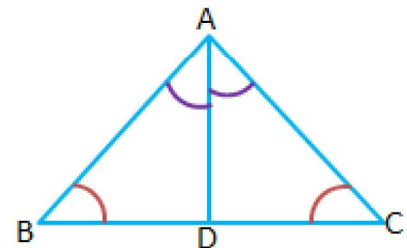
$$\angle B = \angle C \text{ (given)}$$

$$\angle BAD = \angle CAD \text{ (By construction)}$$

$$AD = AD \text{ (Common)}$$

So, $\Delta BAD \cong \Delta CAD$ (By AAS congruence rule)

$$AB = AC \text{ (by CPCT)}$$



Example 4 : In ΔABC , the bisector AD of $\angle A$ is perpendicular to side BC (see Fig. 7.27). Show that $AB = AC$ and ΔABC is isosceles.

Sol: In ΔABD and ΔACD ,

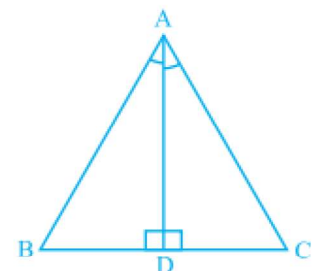
$$\angle BAD = \angle CAD \text{ (Given)}$$

$$AD = AD \text{ (Common)}$$

$$\angle ADB = \angle ADC = 90^\circ \text{ (Given)}$$

So, $\Delta ABD \cong \Delta ACD$ (ASA rule)

So, $AB = AC$ (CPCT) or, ΔABC is an isosceles triangle.



Example 5 : E and F are respectively the mid-points of equal sides AB and AC of ΔABC (see Fig. 7.28). Show that $BF = CE$.

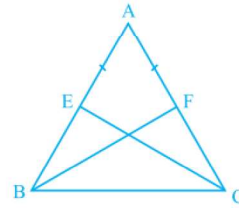
Sol: In $\triangle ABF$ and $\triangle ACE$,

$$AB = AC \text{ (Given)}$$

$$\angle A = \angle A \text{ (Common)}$$

$$AF = AE \text{ (Halves of equal sides)}$$

So, $\triangle ABF \cong \triangle ACE$ (SAS rule) Therefore, $BF = CE$ (CPCT)



Example 6 : In an isosceles triangle ABC with $AB = AC$, D and E are points on BC such that $BE = CD$ (see Fig. 7.29). Show that $AD = AE$.

Sol: In $\triangle ABE$ and $\triangle ACD$,

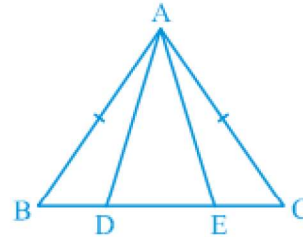
$$AB = AC \text{ (Given)}$$

$$\angle B = \angle C \text{ (Angles opposite to equal sides are equal)}$$

$$BE = CD \text{ (Given)}$$

So, $\triangle ABE \cong \triangle ACD$ (SAS congruence rule)

$$\Rightarrow AE = AD \text{ (CPCT)}$$



EXERCISE 7.1

1. In an isosceles triangle ABC , with $AB = AC$, the bisectors of $\angle B$ and $\angle C$ intersect each other at O . Join A to O . Show that : (i) $OB = OC$ (ii) AO bisects $\angle A$

Sol: (i) In $\triangle ABC$, The bisectors of $\angle B$ and $\angle C$ intersect each other at O

$$\angle OBA = \angle OBC = \frac{1}{2} \angle ABC \text{ and } \angle OCA = \angle OCB = \frac{1}{2} \angle ACB$$

$$\text{Given } AB = AC$$

$$\Rightarrow \angle ABC = \angle ACB \text{ (Angles opposite to equal sides)}$$

$$\Rightarrow \frac{1}{2} \angle ABC = \frac{1}{2} \angle ACB \Rightarrow \angle OBC = \angle OCB$$

$$\text{In } \triangle OBC, \angle OBC = \angle OCB$$

$$\Rightarrow OB = OC \text{ (Sides opposite to equal angles)} \rightarrow (i)$$

(ii) $\triangle OAB$ and $\triangle OAC$

$$OA = OA \text{ (Common)}$$

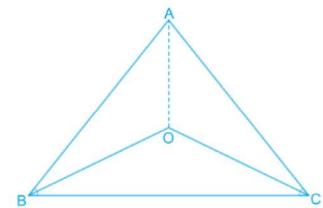
$$AB = AC \text{ (Given)}$$

$$OB = OC \text{ (From (i))}$$

$$\triangle OAB \cong \triangle OAC \text{ (SSS congruence rule)}$$

$$\Rightarrow \angle OAB = \angle OAC \text{ (CPCT)}$$

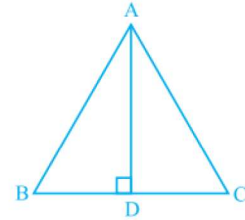
$$\Rightarrow AO \text{ bisects } \angle A$$



2. In $\triangle ABC$, AD is the perpendicular bisector of BC (see Fig. 7.30). Show that $\triangle ABC$ is an isosceles triangle in which $AB = AC$.

Sol: In $\triangle ADB$ and $\triangle ADC$

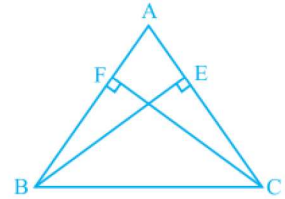
$AD = AD$ (Common)
 $\angle ADB = \angle ADC = 90^\circ$ ($AD \perp BC$)
 $BD = DC$ (AD is bisector of BC)
 $\triangle ADB \cong \triangle ADC$ (SAS congruence rule)
 $\Rightarrow AB = AC$ (CPCT)



3. **ABC is an isosceles triangle in which altitudes BE and CF are drawn to equal sides AC and AB respectively (see Fig. 7.31). Show that these altitudes are equal.**

Sol: $\triangle ABC$ is an isosceles triangle. $AB = AC$

In $\triangle AEB$ and $\triangle AFC$
 $\angle A = \angle A$ (Common angle)
 $\angle AEB = \angle AFC = 90^\circ$ ($BE \perp AC$ and $CF \perp AB$)
 $AB = AC$ (Given)
 $\triangle AEB \cong \triangle AFC$ (AAS congruence rule)
 $\Rightarrow BE = CF$ (CPCT)

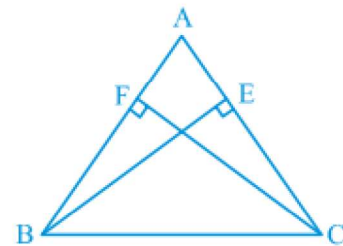


4. **ABC is a triangle in which altitudes BE and CF to sides AC and AB are equal (see Fig. 7.32). Show that**

(i) $\triangle ABE \cong \triangle ACF$ (ii) $AB = AC$, i.e., ABC is an isosceles triangle.

Sol: In $\triangle ABE$ and $\triangle ACF$

$\angle A = \angle A$ (Common angle)
 $\angle AEB = \angle AFC = 90^\circ$ ($BE \perp AC$ and $CF \perp AB$)
 $BE = CF$ (Given)
 $\triangle ABE \cong \triangle ACF$ (AAS Congruence rule)
 (ii) $\triangle ABE \cong \triangle ACF$
 $\Rightarrow AB = AC$ (CPCT)

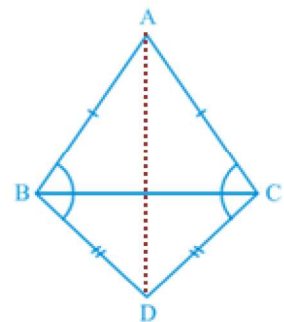


$\triangle ABC$ is an isosceles triangle.

5. **ABC and DBC are two isosceles triangles on the same base BC (see Fig. 7.33). Show that $\angle ABD = \angle ACD$**

Sol: In $\triangle ABD$ and $\triangle ACD$

$AB = AC$ (Given)
 $BD = CD$ (Given)
 $AD = AD$ (Common side)
 $\triangle ABD \cong \triangle ACD$ (SSS Congruence rule)
 $\Rightarrow \angle ABD = \angle ACD$ (CPCT)



6. **$\triangle ABC$ is an isosceles triangle in which $AB = AC$. Side BA is produced to D such that $AD = AB$ (see Fig. 7.34). Show that $\angle BCD$ is a right angle.**

Sol: In $\triangle ABC$, $AB = AC$

$\Rightarrow \angle ABC = \angle ACB = x$ (Angles opposite to equal sides are equal)

In $\triangle ADC$, $AD = AC$

$\Rightarrow \angle ACD = \angle ADC = y$ (Angles opposite to equal sides are equal)

$\angle BCD = \angle ACB + \angle ACD = x + y$

In $\triangle BDC$,

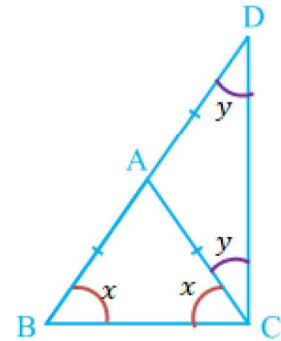
$\angle ABC + \angle ADC + \angle BCD = 180^\circ$ (Angle sum property of a triangle)

$x + y + (x + y) = 180^\circ$

$2(x + y) = 180^\circ$

$(x + y) = \frac{180^\circ}{2} = 90^\circ$

$\angle BCD = 90^\circ$



7. $\triangle ABC$ is a right angled triangle in which $\angle A = 90^\circ$ and $AB = AC$. Find $\angle B$ and $\angle C$.

Sol: In $\triangle ABC$, $AB = AC$

$\Rightarrow \angle C = \angle B = x$ (Equal sides opposite angles are equal)

$\angle A + \angle B + \angle C = 180^\circ$ (Angle sum property of a triangle)

$90^\circ + x + x = 180^\circ$

$2x = 90^\circ$

$x = \frac{90^\circ}{2} = 45^\circ$

$\angle B = \angle C = 45^\circ$

8. Show that the angles of an equilateral triangle are 60° each.

Sol: Let $\triangle ABC$ is an equilateral triangle

$\Rightarrow AB = BC = AC$

$\Rightarrow \angle A = \angle B = \angle C = x$ (Equal sides opposite angles are equal)

$\angle A + \angle B + \angle C = 180^\circ$

$\Rightarrow x + x + x = 180^\circ$

$\Rightarrow 3x = 180^\circ$

$\Rightarrow x = \frac{180^\circ}{3} = 60^\circ$

So, each angle of an equilateral triangle is 60°

SSS congruence rule:

If three sides of one triangle are equal to the three sides of another triangle, then the two triangles are congruent

RHS congruence rule:

If in two right triangles the hypotenuse and one side of one triangle are equal to the hypotenuse and one side of the other triangle, then the two triangles are congruent.

Example 7 : AB is a line-segment. P and Q are points on opposite sides of AB such that each of them is equidistant from the points A and B (see Fig. 7.37). Show that the line PQ is the perpendicular bisector of AB .

Sol: In ΔPAQ and ΔPBQ .

$$PA = PB \text{ (Given)}$$

$$AQ = BQ \text{ (Given)}$$

$$PQ = PQ \text{ (Common)}$$

$$\Delta PAQ \cong \Delta PBQ \text{ (SSS rule)}$$

$$\angle APQ = \angle BPQ \text{ (CPCT)} \Rightarrow \angle APC = \angle BPC \rightarrow (1)$$

In ΔPAC and ΔPBC .

$$AP = BP \text{ (Given)}$$

$$\angle APC = \angle BPC \text{ (From (1))}$$

$$PC = PC \text{ (Common)}$$

$$\Delta PAC \cong \Delta PBC \text{ (SAS rule)}$$

$$AC = BC \text{ (CPCT)} \rightarrow (2)$$

$$\angle ACP = \angle BCP \text{ (CPCT)}$$

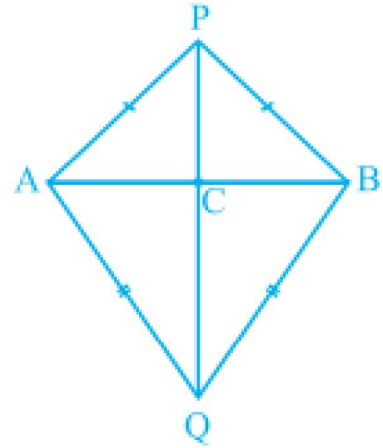
$$\angle ACP + \angle BCP = 180^\circ \text{ (Linear pair)}$$

$$2\angle ACP = 180^\circ$$

$$\angle ACP = 90^\circ \rightarrow (3)$$

From (2) and (3)

PQ is perpendicular bisector of AB



Example 8 : P is a point equidistant from two lines l and m intersecting at point A (see Fig. 7.38). Show that the line AP bisects the angle between them.

Sol: Let $PB \perp l$, $PC \perp m$. It is given that $PB = PC$

In ΔPAB and ΔPAC

$$\angle PBA = \angle PCA = 90^\circ \text{ (Given)}$$

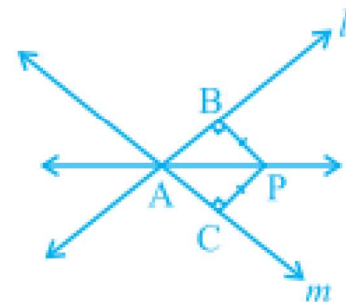
$$PA = PA \text{ (Common)}$$

$$PB = PC \text{ (Given)}$$

$$\Delta PAB \cong \Delta PAC \text{ (RHS rule)}$$

$$\angle PAB = \angle PAC \text{ (CPCT)}$$

AP bisects the angle between l and m



EXERCISE 7.3

1. $\triangle ABC$ and $\triangle DBC$ are two isosceles triangles on the same base BC and vertices A and D are on the same side of BC (see Fig. 7.39). If AD is extended to intersect BC at P , show that
 (i) $\triangle ABD \cong \triangle ACD$ (ii) $\triangle ABP \cong \triangle ACP$ (iii) AP bisects $\angle A$ as well as $\angle D$. (iv) AP is the perpendicular bisector of BC .

Sol: (i) In $\triangle ABD$ and $\triangle ACD$

$$AB = AC \text{ (Given)}$$

$$BD = CD \text{ (Given)}$$

$$AD = AD \text{ (Common)}$$

$$\triangle ABD \cong \triangle ACD \text{ (SSS rule)}$$

$$\angle BAD = \angle CAD \text{ (CPCT)}$$

$$\text{i.e. } \angle BAP = \angle CAP \rightarrow (1)$$

(ii) $\triangle ABP \cong \triangle ACP$

$$AB = AC \text{ (Given)}$$

$$\angle BAP = \angle CAP \text{ (From (1))}$$

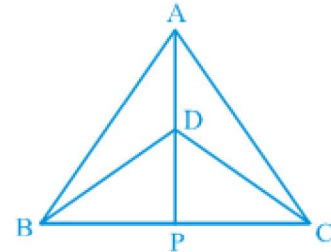
$$AP = AP \text{ (Common)}$$

$$\triangle ABP \cong \triangle ACP \text{ (SAS rule)}$$

$$\angle APB = \angle APC \text{ (CPCT)} \rightarrow (2)$$

$$\text{i.e. } \angle DPB = \angle DPC \rightarrow (3)$$

$$\text{Also } BP = PC \text{ (CPCT)} \rightarrow (4)$$



(iii) From (1) and (2)

AP bisects $\angle A$ as well as $\angle D$

(iv) $\angle APB + \angle APC = 180^\circ$ (Linear pair)

From (2); $\angle APB = \angle APC$

$$\therefore \angle APB = \angle APC = 90^\circ \rightarrow (5)$$

(iv) From (4) and (5)

AP is the perpendicular bisector of BC .

2. AD is an altitude of an isosceles triangle ABC in which $AB = AC$. Show that (i) AD bisects BC (ii) AD bisects $\angle A$.

Sol: In $\triangle ADB$ and $\triangle ADC$

$$AB = AC \text{ (Given)}$$

$$\angle ADB = \angle ADC = 90^\circ \text{ (} AD \perp BC \text{)}$$

$$AD = AD \text{ (Common)}$$

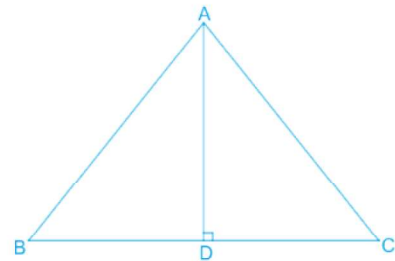
$$\triangle ADB \cong \triangle ADC \text{ (RHS Congruence rule)}$$

$$BD = CD \text{ (CPCT)}$$

Hence, AD bisects BC

$$\angle BAD = \angle CAD \text{ (CPCT)}$$

AD bisects $\angle A$



3. Two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of $\triangle PQR$ (see Fig. 7.40). Show that (i) $\triangle ABM \cong \triangle PQN$ (ii) $\triangle ABC \cong \triangle PQR$

Sol: In $\triangle ABC$, AM is median

$$BM = CM = \frac{1}{2} BC$$

In ΔPQR , PN is median

$$QN = NR = \frac{1}{2}QR$$

Given $BC=QR$

$$\frac{1}{2}BC = \frac{1}{2}QR$$

$$BM = QN \rightarrow (1)$$

(i) $\Delta ABM \cong \Delta PQN$

$AB = PQ$ (Given)

$AM = PN$ (Given)

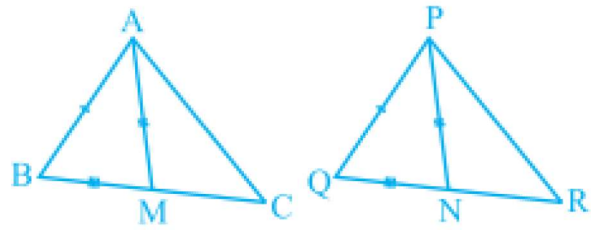
$BM = QN$ (From(1))

$\Delta ABM \cong \Delta PQN$ (SSS rule)

$$BM = QN \rightarrow (1)$$

$\angle ABM = \angle PQN$ (CPCT)

$$\angle ABC = \angle PQR \rightarrow (2)$$



(ii) In ΔABC and ΔPQR

$AB = PQ$ (Given)

$\angle ABC = \angle PQR$ (From(2))

$BC = QR$ (Given)

$\Delta ABC \cong \Delta PQR$ (ASA rule)

4. **BE and CF are two equal altitudes of a triangle ABC. Using RHS congruence rule, prove that the triangle ABC is isosceles.**

Sol: In ΔBEC and ΔCFB

$\angle BEC = \angle CFB = 90^\circ$ (BE and CF are two altitudes)

$BC = BC$ (Common)

$BE = CF$ (Given)

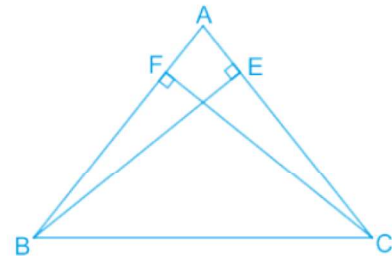
$\Delta BEC \cong \Delta CFB$ (RHS rule)

$\angle BCE = \angle CBF$ (CPCT)

i.e, $\angle BCA = \angle CBA$

$AB=AC$ (Sides opposite to equal angles are equal)

Hence, ΔABC is isosceles triangle.



5. **ABC is an isosceles triangle with $AB = AC$. Draw $AP \perp BC$ to show that $\angle B = \angle C$.**

Sol: In ΔAPB and ΔAPC

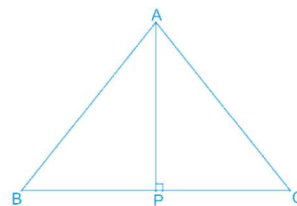
$\angle APB = \angle APC = 90^\circ$

$AB = AC$

$AP = AP$ (Common)

$\Delta APB \cong \Delta APC$ (RHS rule)

$\angle B = \angle C$ (CPCT)



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